

# Simulation of Gravity-Driven Flow Through a Microfluidic Device on a Rocker Platform

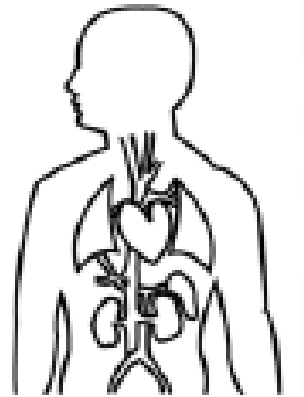
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<sup>1</sup>University of Central Florida, Orlando, FL

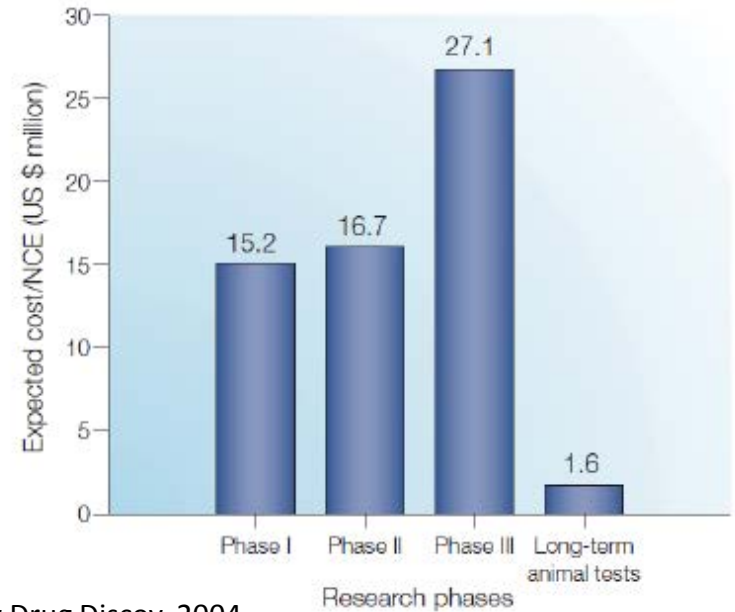
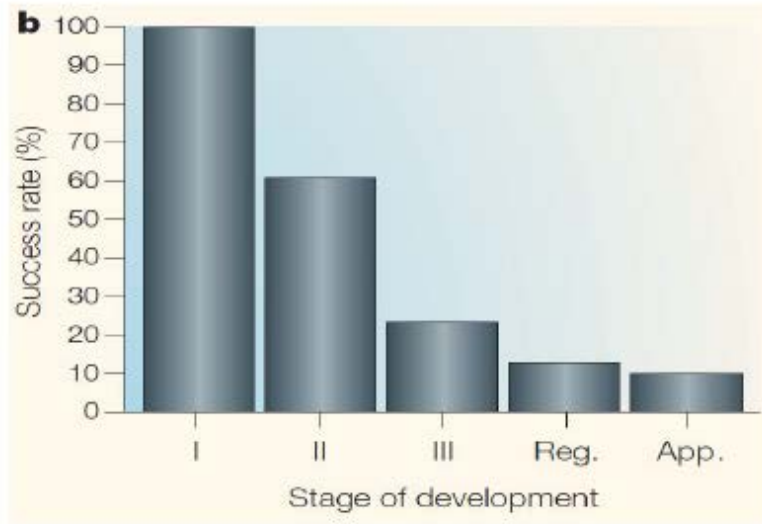
<sup>2</sup>Cornell University, Ithaca, NY

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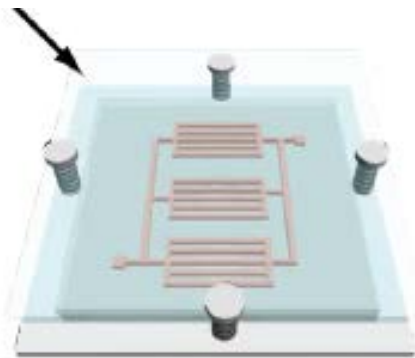
# Drug development costs and microscale cell culture analog( $\mu$ CCA)



Human body  
(in vivo)



Kola & Landis, Nat Rev Drug Discov, 2004  
Dickson, Nat Rev Drug Discov, 2004

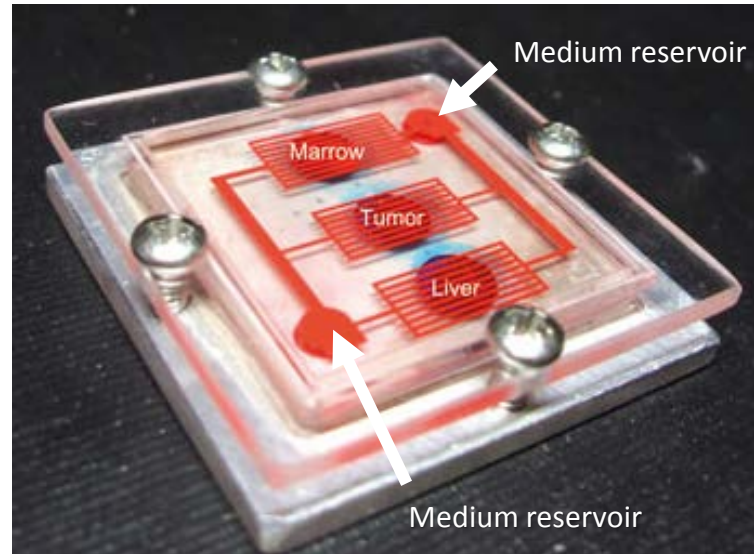


Microscale cell culture analog  
(in vitro)

Shuler Lab, Cornell University

- 1 in 10 drugs entering phase 1 gets approved
- Testing is expensive and time consuming
- Ethical issue: Animal testing

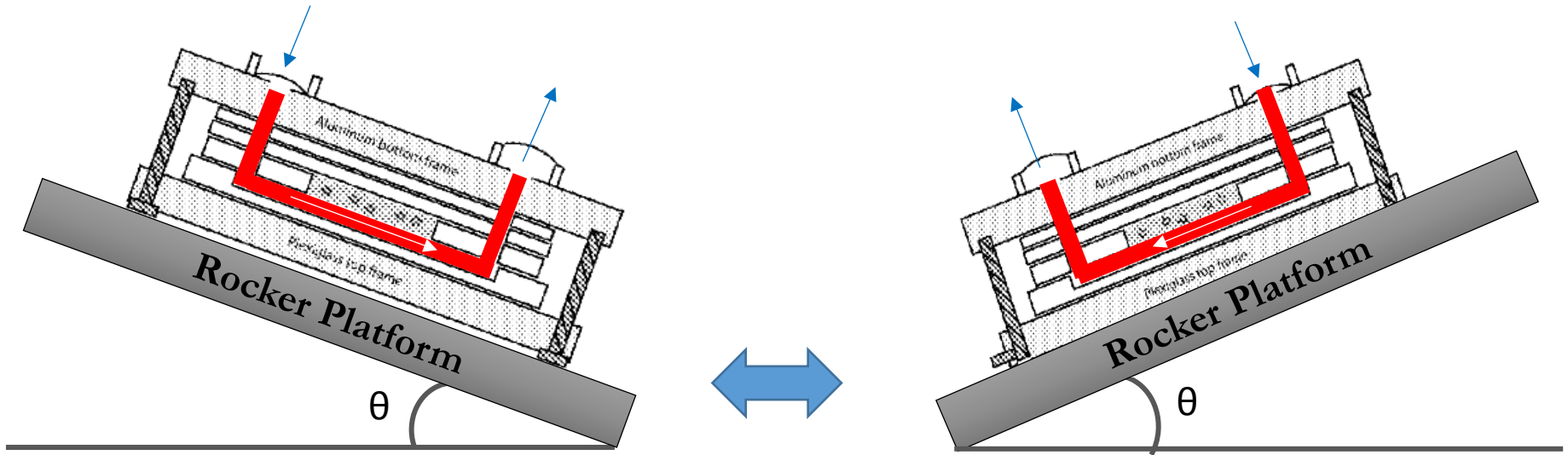
# Simulations: Need?



μCCA for 3D cell culture, Shuler Lab, Cornell University

- Microfluidic device for organ-on-chip applications
- Drug testing
  - Drug diffusion and consumption
- Oxygen consumption
  - Hypoxia
- Cells are subjected to shear stress – mechanotransduction
  - Morphology, physiology
  - Physiological shear stress range – organ dependent
  - Shear stress estimation
  - Flow rates and velocity

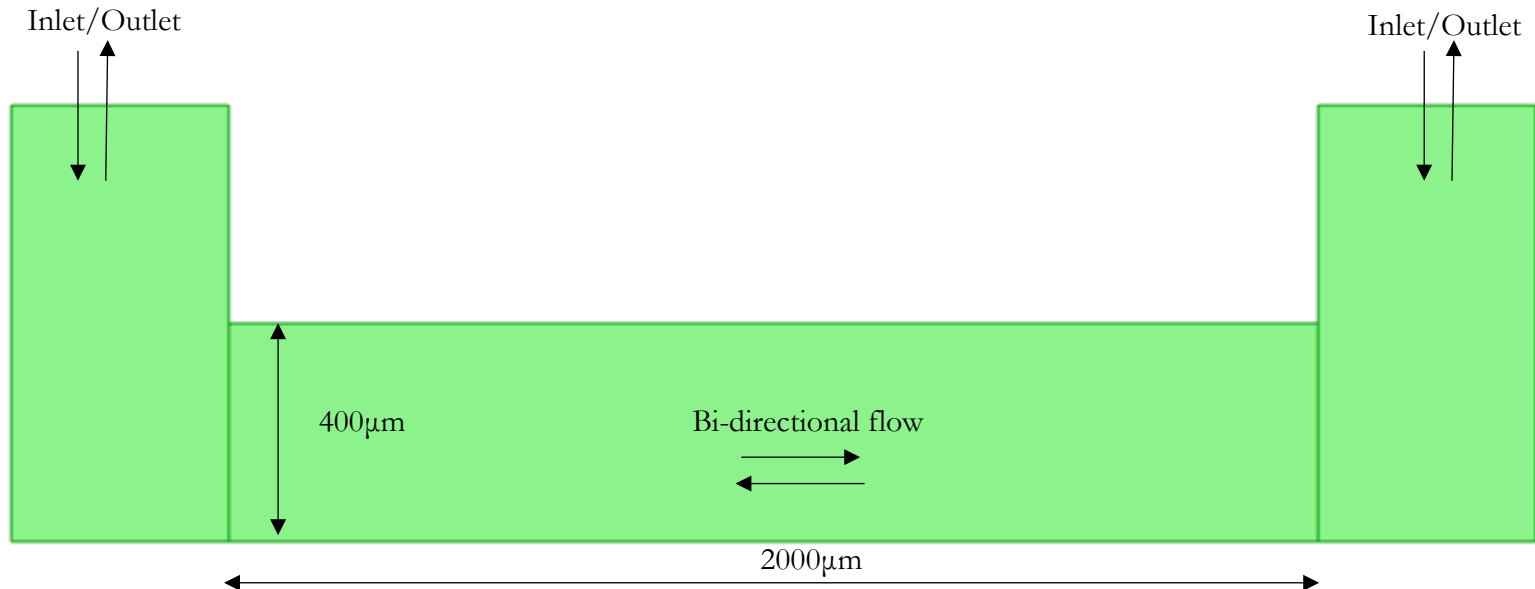
# Gravity-driven flow through a microfluidic device



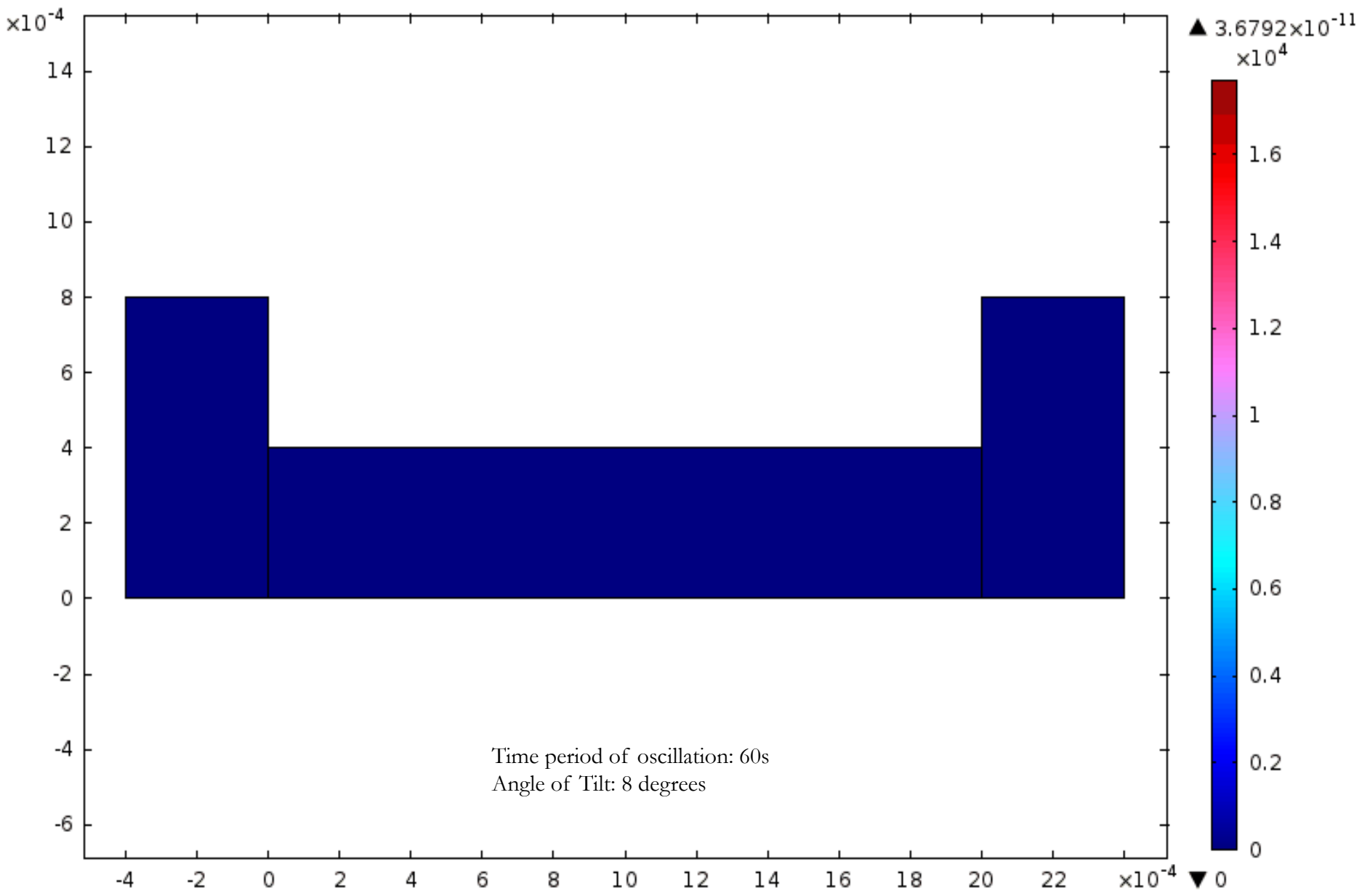
- Medium is recirculated by reciprocating tilting with rocker platform
- Gravity-induced flow naturally eliminates bubble problem
- No external pumps and tubing – reduces footprint of the device

# Simulation of gravity driven bi-directional flow

- Module: Fluid flow → “Laminar Flow”
  - Incompressible flow, cell culture medium (viscosity, density)
- gravitational body force
  - Variable: frequency of oscillation
  - Angle of Tilt



Surface: Velocity magnitude ( $\mu\text{m/s}$ ) Arrow Surface: Velocity field



# Oxygen consumption within tissue

- Oxygen consumption rate in tissue: follows Michaelis-Menten type reaction

- $R = K_{\max} * C / (C + M)$

- $K_{\max} = 0.034 \text{ mol/m}^3/\text{s}$  (max. O<sub>2</sub> consumption rate)

- $M = \text{Michaelis-Menten constant; } = 1.0 \times 10^{-3} \text{ mol/m}^3$



Vary with tissue type

- Oxygen concentrations and diffusion:

- $C_{\text{atm}} = 0.200 \text{ mol/m}^3$

- $C_{\text{tissue}} \text{ initial} = 0.05 \text{ mol/m}^3$

- Diffusion Constants:

- $D_w = 3.0 \times 10^{-9} \text{ m}^2/\text{s}$  (O<sub>2</sub> in water);

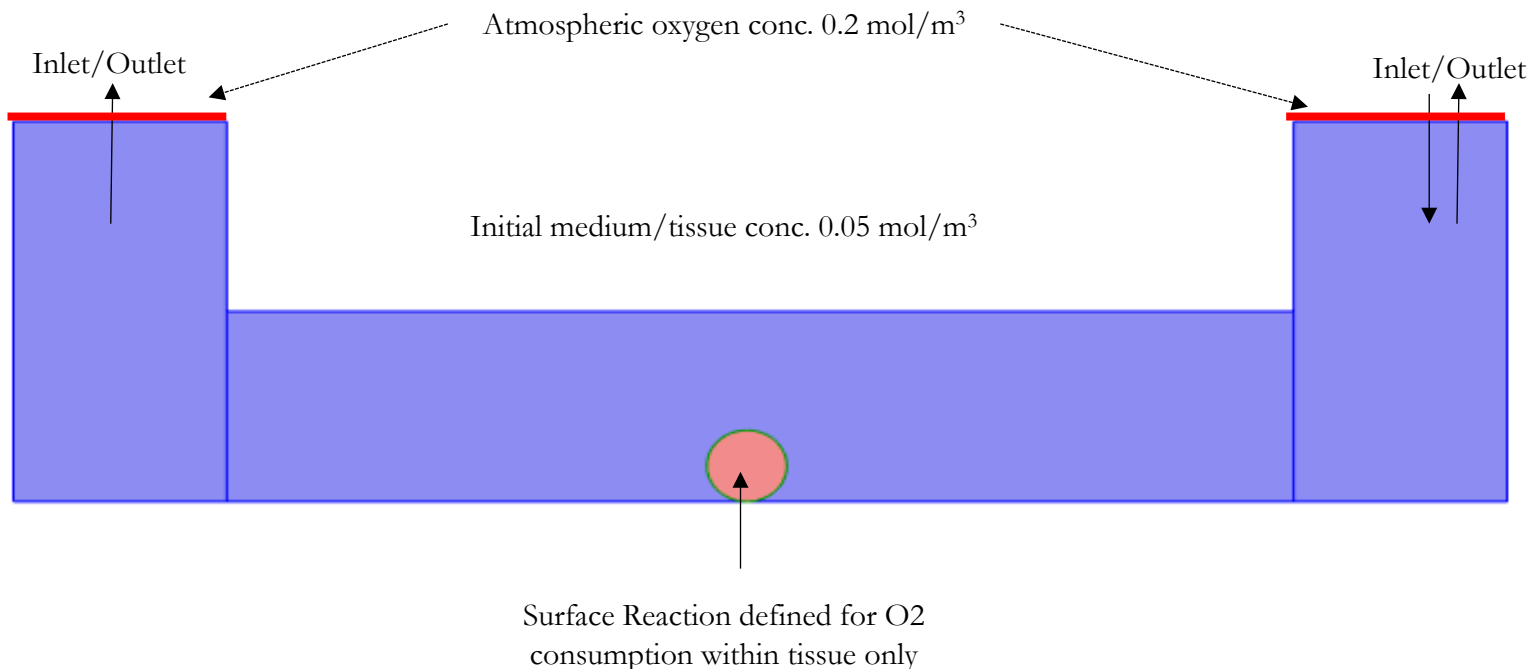
- $D_t = 2.0 \times 10^{-9} \text{ m}^2/\text{s}$  (O<sub>2</sub> in tissue)

# Simulation of gravity driven bi-directional flow with oxygen diffusion and consumption in a tissue

- Module:

Chemical Reaction Engineering → “Transport of dilute species” + Fluid flow → “Laminar Flow”

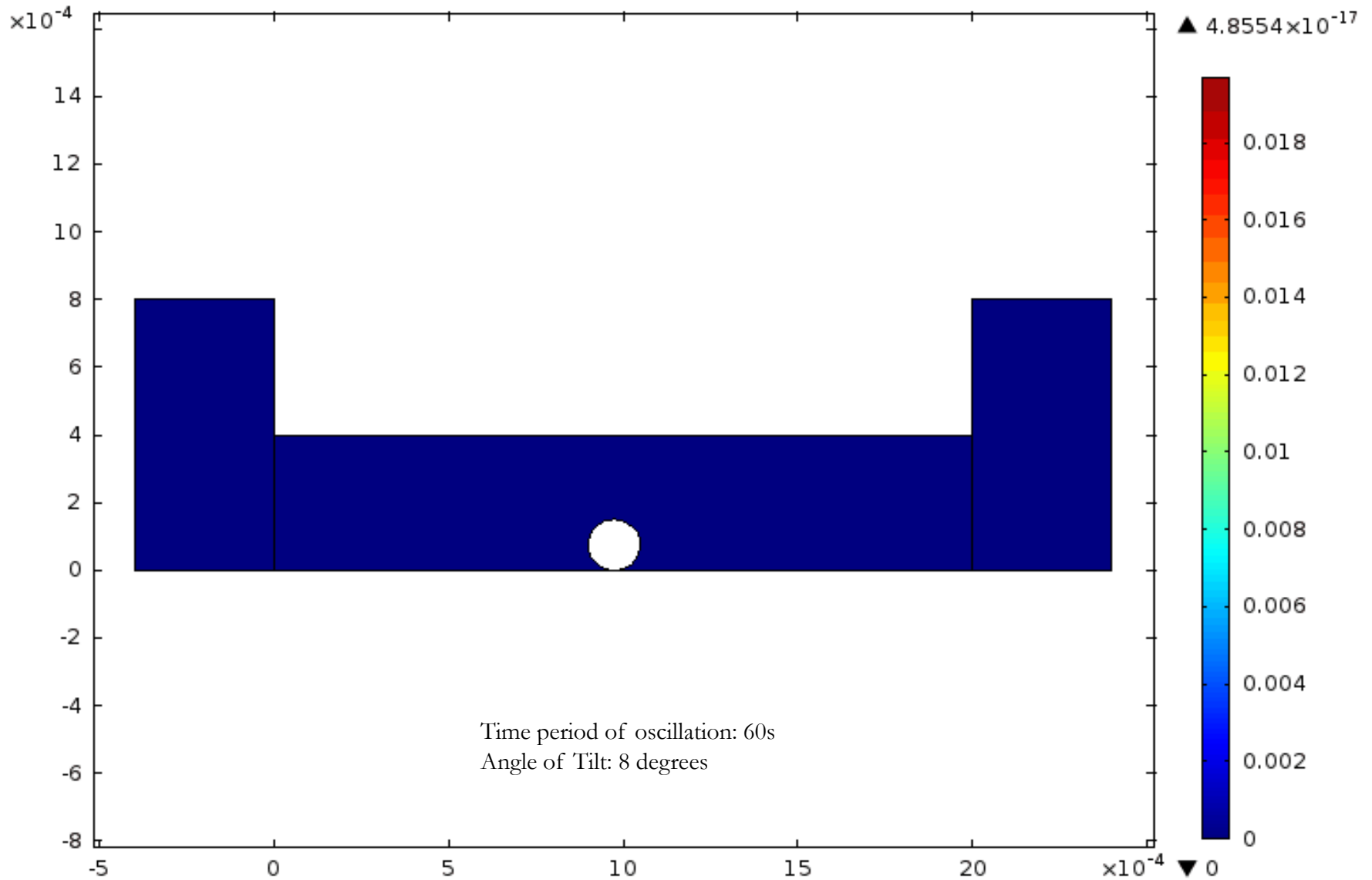
- Solve flow first and then use flow results as input for transport of dilute species





# Bi-directional flow around the tissue

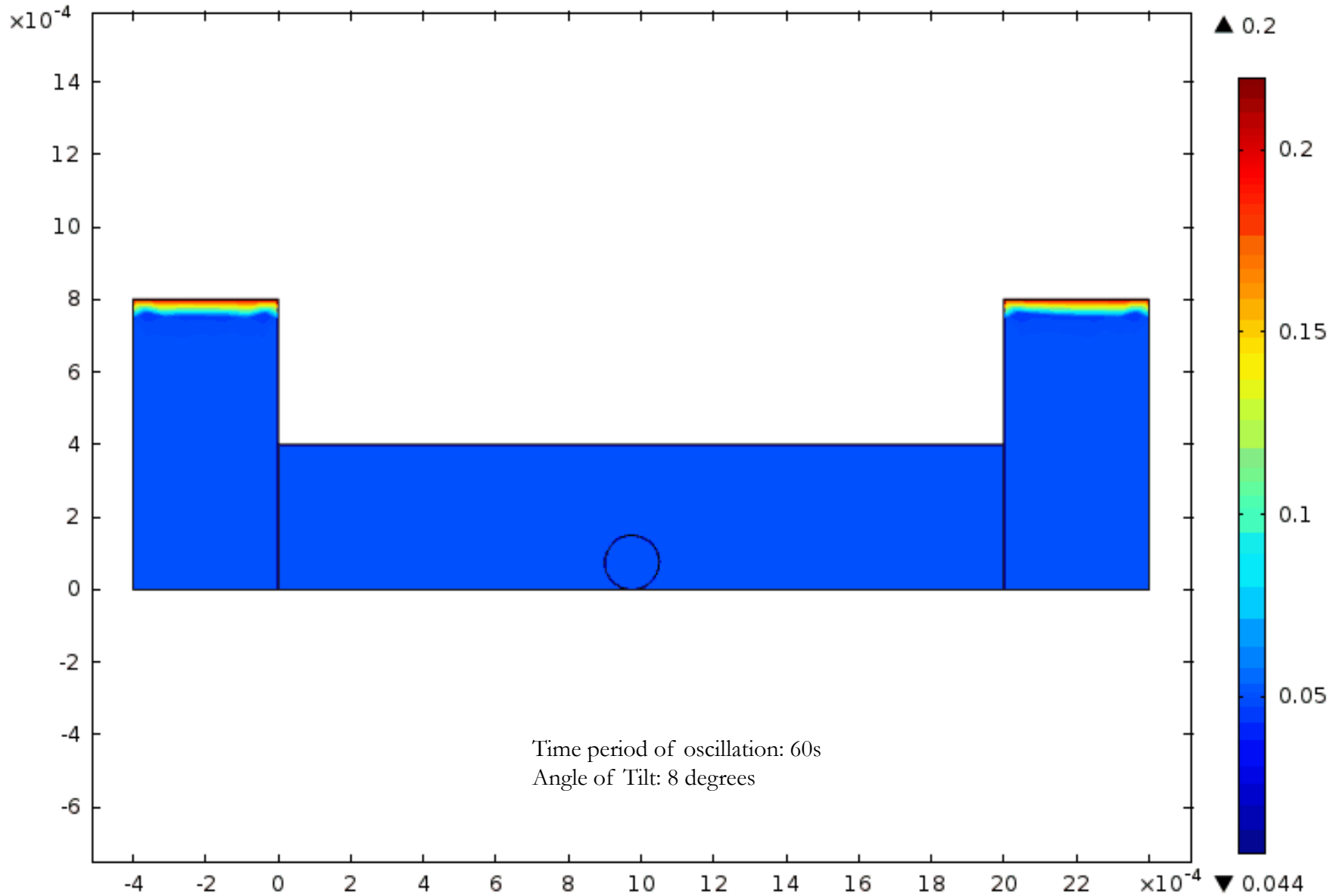
Surface: Velocity magnitude (m/s) Arrow Surface: Velocity field



# Bi-directional flow around the tissue

## Oxygen diffusion and consumption

Surface: Concentration (mol/m<sup>3</sup>) Arrow Surface: Total flux



# Drug diffusion and consumption within tissue

## Simulation Approach

- Drug consumption rate in tissue: follows Michaelis-Menten type reaction

- $R = K_{\max} * C / (C + M)$

- $K_{\max}$  (max. drug consumption rate)

- $M$  = Michaelis-Menten constant

Vary with tissue/enzyme/drug combination

- Oxygen concentrations and diffusion:

- $C_{\text{drug}}$  and  $C_{\text{tissue}}$

- Diffusion Constants:

- $D_w$  (drug in culture medium);

- $D_t$  (drug in tissue)

# Conclusions

- Simulation models
  - Bi-directional gravity driven flow
  - Diffusion
  - Consumption of oxygen/ drugs in tissue based on Michaelis-Menten type Reactions
- Design of microfluidic systems
  - Physiological shear stress
  - Drug diffusion times
  - Drug concentration/distribution within the device
  - Drug consumption rates