

Technical University of Cluj-Napoca, Romania
Department of Electrotechnics and Measurements

Analysis Of Linearly Polarized Modes

Ioana Moldovean (Avram), Ioan G. Tarnovan , Bogdan Tebrea

Introduction

- This paper is an analysis of the propagation mode of step index fiber optic
- To obtain the propagation modes of electromagnetic waves the characteristics of the optical fiber has been changed
- Analytical method of this analysis is based on finite element method
- This study is required for further investigation of states of polarization and analysis of electric field distribution

Basic equations

- Snell's law: $n_1 \sin \phi_1 = n_2 \sin \phi_2$
- Wave equation: $A(r, t) = \text{Re}\{\bar{A}(r) \exp(j\omega t)\}$
- The equation of electric field:
$$\nabla^2 E + \nabla \left(\frac{\nabla \epsilon_r}{\epsilon_r} \cdot E \right) + k^2 E = 0$$
$$\nabla^2 E + k^2 E = 0$$
- The equation for magnetic field:
$$\nabla^2 H + \frac{\nabla \epsilon_r}{\epsilon_r} \times (\nabla \times H) + k^2 H = 0$$
$$\nabla^2 H + n^2 k_0^2 H = 0$$
- The Helmholtz's equation for the electric and magnetic fields can be summarized as

$$\nabla_{\perp}^2 E + (k^2 - \beta^2) E = 0$$

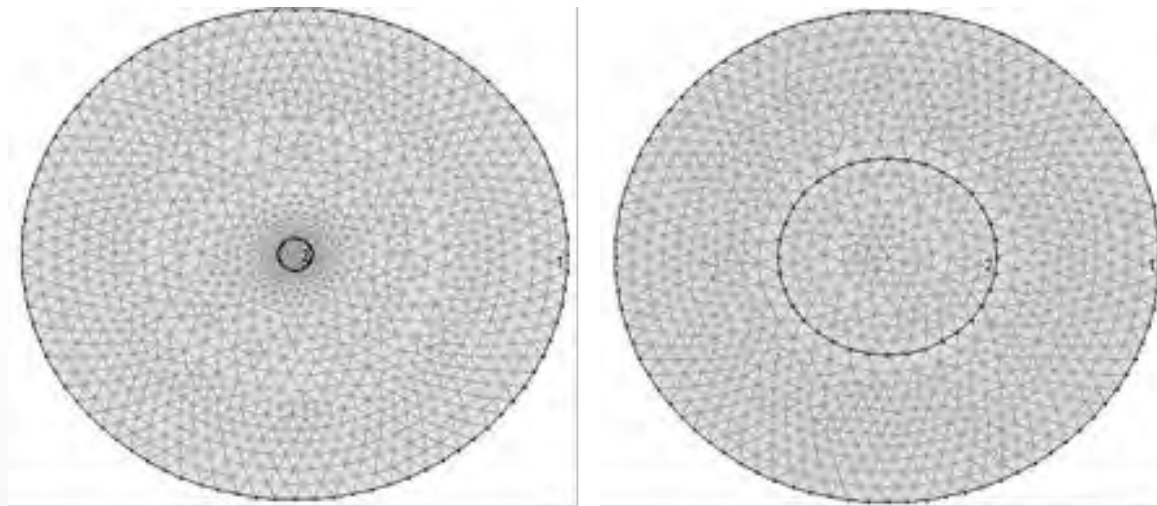
$$\nabla_{\perp}^2 E + k_0^2 (\epsilon_r - n_{eff}^2) E = 0$$

$$\nabla_{\perp}^2 H + (k^2 - \beta^2) H = 0$$

$$\nabla_{\perp}^2 H + k_0^2 (\epsilon_r - n_{eff}^2) H = 0$$

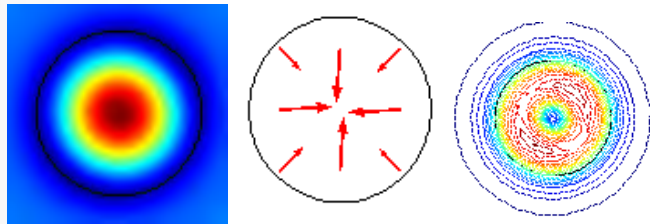
The propagation of electromagnetic field

- Optical fibers
 - core- 8 μm and 50 μm
 - cladding - 125 μm
 - Refractive index of core – 1.4457
 - Refractive index of cladding – 1.4378
 - Core – pure silica
 - Cladding – doped silica

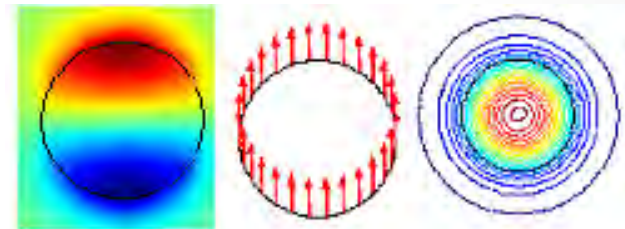


Finite element mesh for single mode and multimode fiber optic

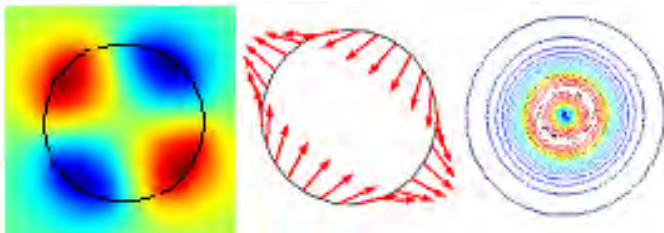
Classification of LP_{nm} modes for single mode optical fiber and the distribution of electric and magnetic field



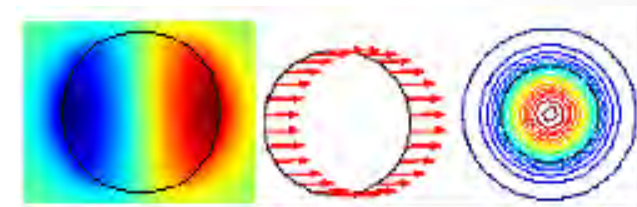
Fundamental mode



LP_{01} Electric transverse mode

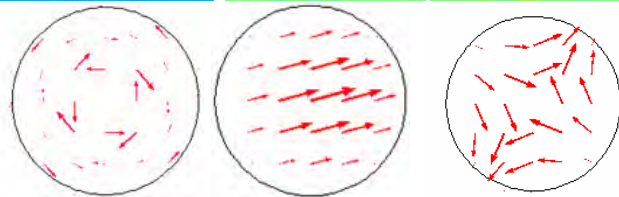
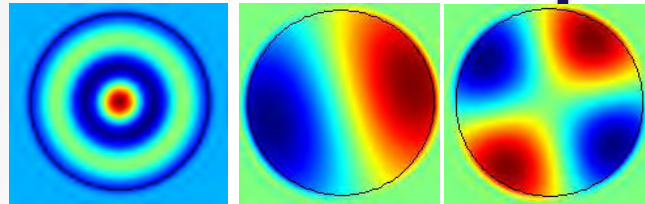


LP_{02} mode

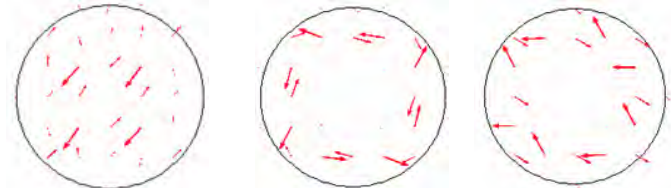
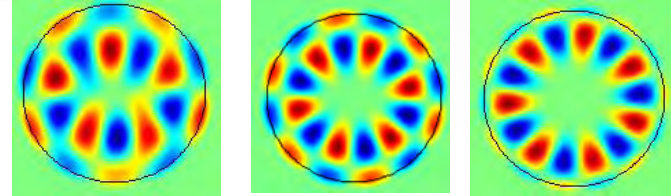


LP_{01} Magnetic transverse mode

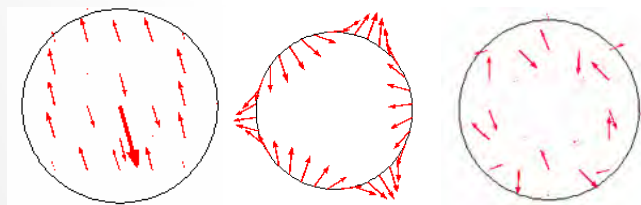
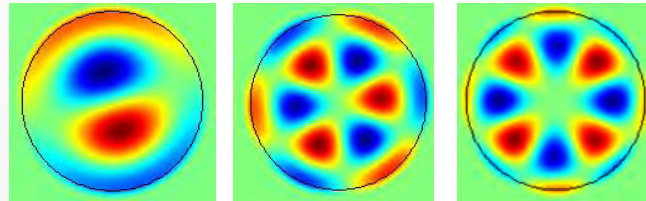
Classification of LP_{nm} modes and distribution of electric field for multimode optical fiber



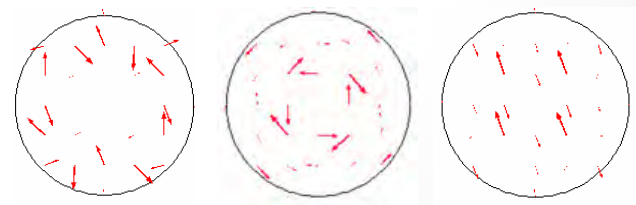
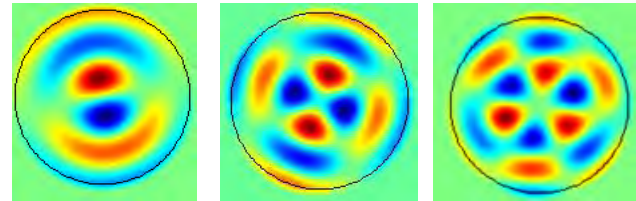
$LP_{01}, LP_{11}, LP_{21}$



$LP_{52}, LP_{62}, LP_{72}$

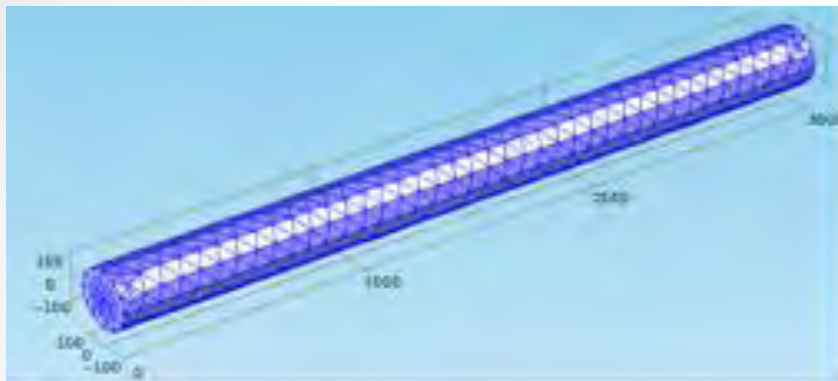


$LP_{12}, LP_{32}, LP_{42}$

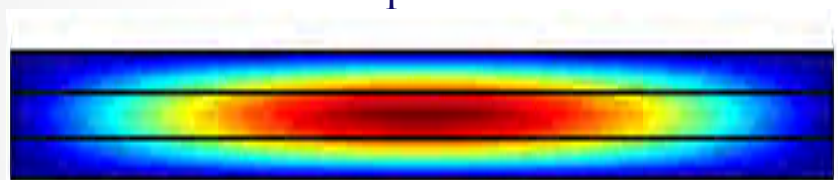


$LP_{13}, LP_{23}, LP_{33}$

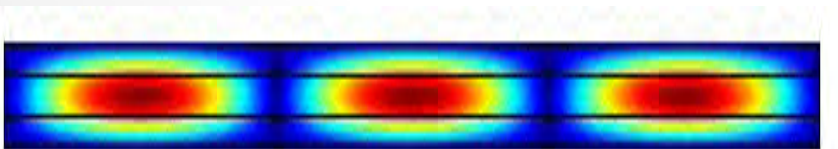
The propagation of electromagnetic wave through a transversal optical fiber.



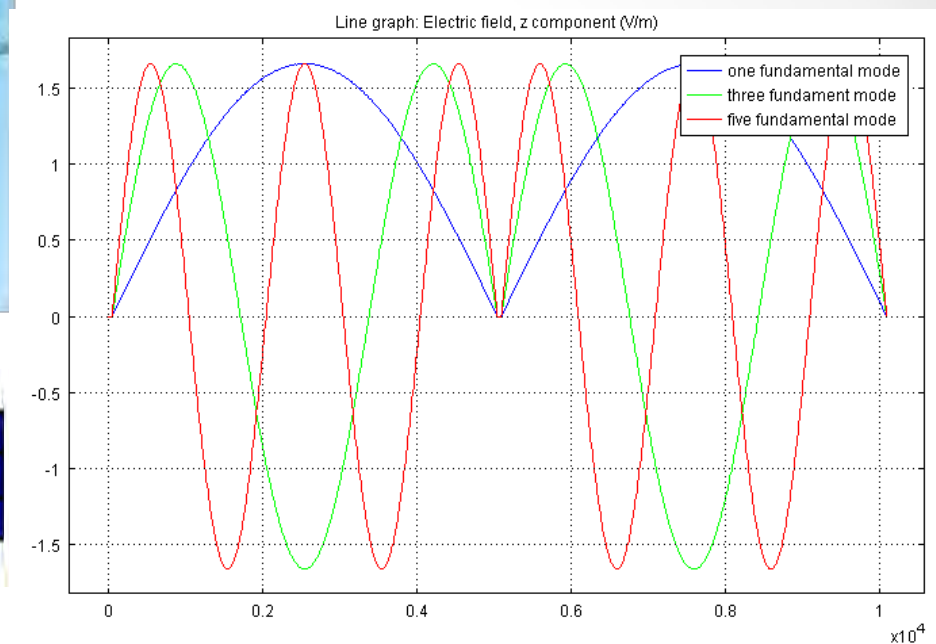
The 3-D optical fiber



The electrical field distribution
One fundamental mode

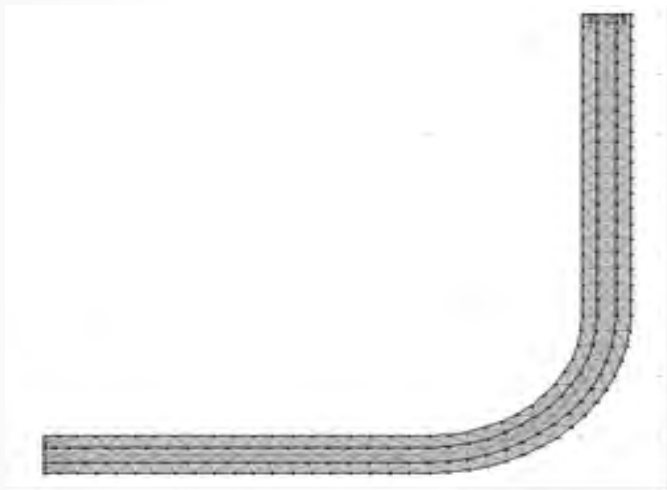


The electrical field distribution.
Three fundamental modes



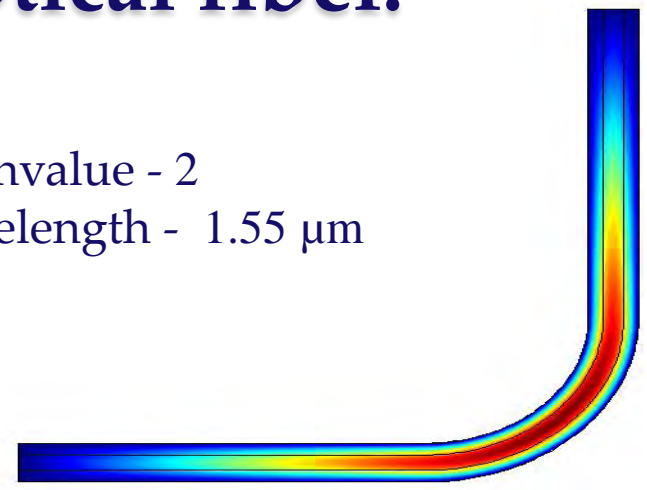
Line graph for electric field distribution along
the z axis

The propagation of electromagnetic wave through a curved optical fiber.



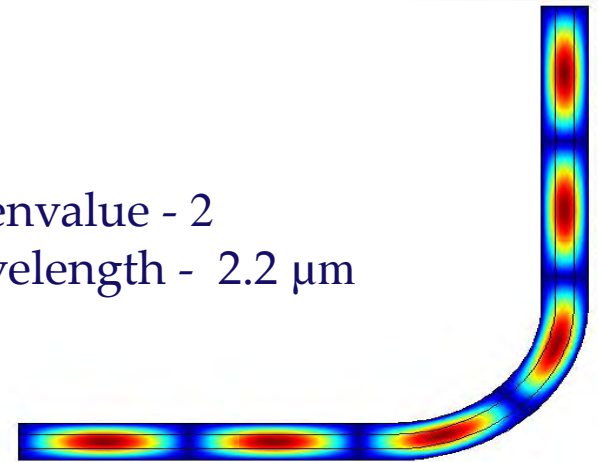
The mesh for the multimode curved optical fiber

Eigenvalue - 2
Wavelength - $1.55 \mu\text{m}$



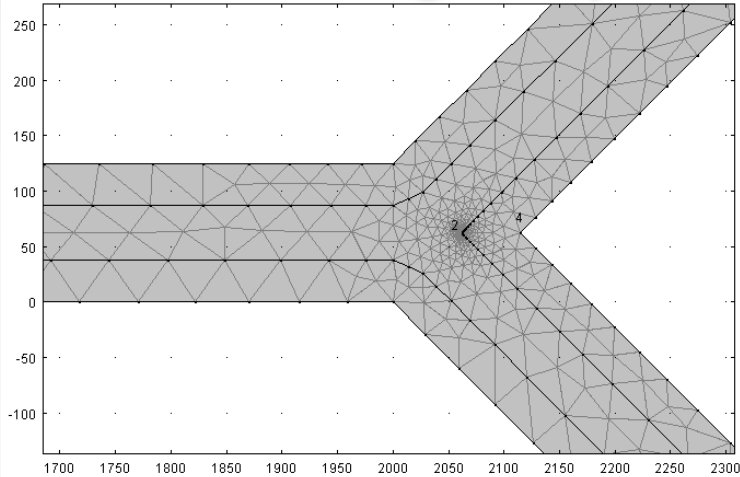
The electric field .
One fundamental LP

Eigenvalue - 2
Wavelength - $2.2 \mu\text{m}$

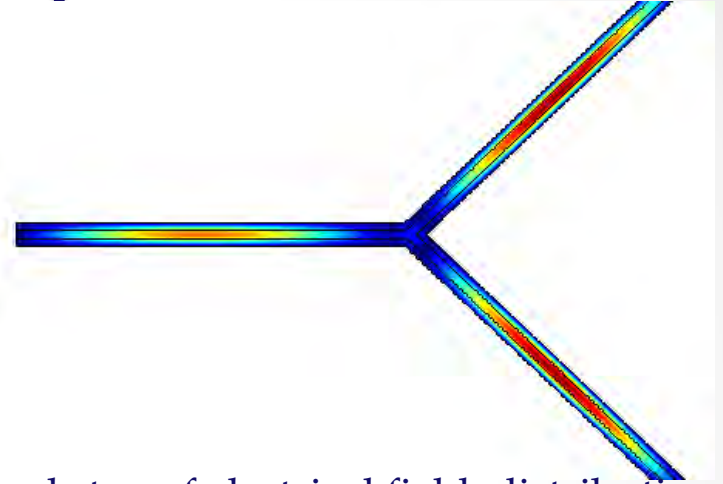


The electric field
Six fundamental LP

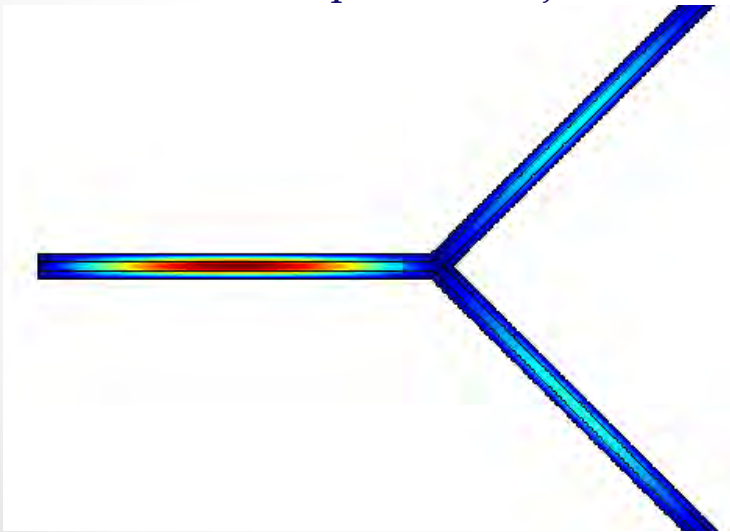
The propagation of electromagnetic wave through a junction optical fiber



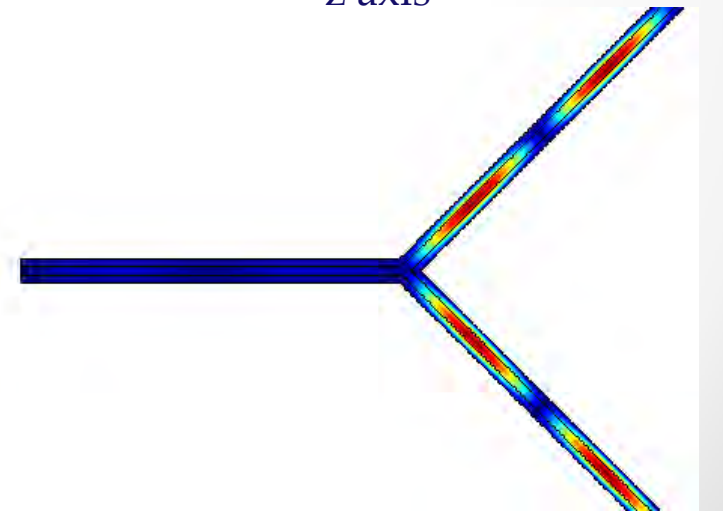
The mesh of optical fiber junction



Second step of electrical field distribution along z axis



First step of electrical field distribution along z axis



Last step of electrical field distribution along z axis

Conclusion

- According to the simulation through the single-mode fiber, the wave is transmitted in one linearly polarized mode
- Through the multimode fiber more light waves can pass, but each with its particular linearly polarized mode
- These simulations will be developed to simulate Faraday Effect, Kerr Effect and Pockels Effect